

**CECS 528, Learning Outcome Assessment 8b, April 7th, Spring 2023,
Dr. Ebert**

NO NOTES, BOOKS, ELECTRONIC DEVICES, OR INTERPERSONAL COMMUNICATION ALLOWED. Submit solutions to at most 2 LO problems on separate sheets of paper.

Problems

LO4. Use the Master method to determine the growth of $T(n)$ if it satisfies $T(n) = 3T(n/2) + n \log n$.

LO5. Recall that the **Maximum Subsequence Sum (MSS)** problem (Exercise 34) admits a divide-and-conquer algorithm that, on input integer array a , requires computing the maximum of $MSS_{\text{left}}(a)$, $MSS_{\text{right}}(a)$, and $MSS_{\text{mid}}(a)$. If the array is

$$a = -1, 3, -2, 5, -5, 0, 1, 4, 2, -4, -3$$

then

- (a) Provide $MSS_{\text{left}}(a)$, $MSS_{\text{right}}(a)$. Hint: no need to show work!
- (b) Provide the two arrays of sums, Sum_{left} and $\text{Sum}_{\text{right}}$ that are used to compute $MSS_{\text{mid}}(a)$. Explain how to compute $MSS_{\text{mid}}(a)$ from these two arrays.

LO6. Given that $r = ae + bg$, $s = af + bh$, $t = ce + dg$, and $u = cf + dh$ are the four entries of AB , and Strassen's products are obtained from matrices

$$A_1 = a, B_1 = f - h, A_2 = a + b, B_2 = h, A_3 = c + d, B_3 = e, A_4 = d, B_4 = g - e,$$

$$A_5 = a + d, B_5 = e + h, A_6 = b - d, B_6 = g + h, A_7 = a - c, B_7 = e + f,$$

Compute P_1, \dots, P_7 and use them to compute r, s, t , and u .

LO7. Answer/Solve the following questions/problems.

- (a) The dynamic-programming algorithm that solves the **Optimal Binary Search Tree** optimization problem defines a recurrence for the function $wac(i, j)$. In words, what does $wac(i, j)$ equal? Hint: do *not* write the recurrence (see Part b).
- (b) Provide the dynamic-programming recurrence for $wac(i, j)$.
- (c) Apply the recurrence from Part b to the set of weights 40, 40, 10, 20 (for keys 1-4, respectively). Show the matrix of subproblem solutions and use it to provide an optimal bst.

LO8. Answer/Solve the following questions/problems.

- (a) The dynamic-programming algorithm that solves the **Traveling Salesperson** optimization problem (Exercise 30 from the Dynamic Programming Lecture) defines a recurrence for the function $mc(i, A)$. In words, what does $mc(i, A)$ equal? Hint: do *not* write the recurrence (see Part b).
- (b) Provide the dynamic-programming recurrence for $mc(i, A)$.
- (c) Apply the recurrence from Part b to the graph below. Show all the necessary computations.

