

## Homework Sections 6.3.

*Due Thursday, November 9*

I. This question refers to problem #41 on page 349, which uses research published in a journal called *Archives of Disease in Children* in 1997.

A. What are the units on  $w$ ,  $R(w)$ , and  $R'(w)$ ?

B. Do part (a). Don't forget that the log is base 10, so when you differentiate, use the appropriate formula. After you use implicit differentiation, solve for  $R'(w)$ . Your answer will have an  $R(w)$  in it. Substitute in the simplified version of  $R(w)$  that you found in part B above to complete your answer.

C. Do part (b). Solve for  $R(w)$  by raising 10 to the power of each side of the equation, and differentiate using the chain rule (carefully).

D. Write a paragraph to answer the question in part (c), including each of the following.

1. Briefly explain the steps to finding  $R'(w)$  in each case.

2. For this problem, which method is more efficient, and why?

3. In problems #1-18 on page 347, an equation with variables  $x$  and  $y$  is given, and the question is to find  $dy/dx$ . Make up two example problems of this form, one in which it is easier to find  $dy/dx$  by solving for  $y$  and then differentiating, and one in which it is easier to find  $dy/dx$  by using implicit differentiation and then solving for  $dy/dx$ .

E. By the way: The formula for  $R(w)$  in this problem is not written in the simplest way. Solve for  $R(w)$  and then use the laws of logs and exponents to put your answer in the form  $R(w) = Kw^m$  where  $K$  and  $m$  are numbers. Now find  $R'(w)$ , using the power rule.

II. The equation for a circle centered at the origin with radius 6 is  $x^2 + y^2 = 36$ .

A. Find the points on the circle with  $x$  coordinate equal to 4. In other words, find  $y$  so that  $(4,y)$  satisfies the equation of the circle.

B. Write the equation for the tangent line at each of the points you found in part (A).

C. Draw a graph of the circle and the tangent lines. Label the points and the  $y$ -intercepts of the tangent lines with their coordinates.